LEVELS K-Algebra 1

Eureka Math² ™ Reviewer Rubric

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Eureka Math²: Alignment at a Glance Criteria of High-Quality, Effective Math Programs	Meets Criteria	
	Yes	No
1. Content and Focus		
A. Curricular materials align with standards and are mathematically accurate. i. Sufficient time and resources are allocated to ensure the materials meet the full intent of grade-level standards.		
B. Curricular materials focus on major work of each grade level.		
C. Curricular materials connect supporting and additional work to major work in meaningful ways. i. Curricular materials make natural connections between different clusters and domains.		
2. Coherence and Instructional Design		
A. Curricular materials use a logical mathematical progression to build on learning from prior content.		
B. Coherent high-yield models are evident within and across grade levels.		
C. Curricular materials include an intentional sequence for developing academic and mathematical language within and across grade-level courses.		
D. Curricular materials utilize a consistent module and lesson structure, including a variety of well-designed teacher-facilitated experiences.		
E. Students' ideas are valued and seen as resources for learning.		
F. Curricular materials build knowledge of not only key ideas in mathematics but also knowledge of the world.		
G. Curricular materials are research-based.		
3. Balance of Rigor		
A. Curricular materials contain a balance of conceptual understanding, procedural skills, and fluency, as well as application of math knowledge.		
B. Curricular materials support the development of students' conceptual understanding with i. simple–to–complex problem sequences ii. concrete–pictorial–symbolic progressions and connections		
C. Curricular materials are designed so that students attain the procedural skills and fluency required by grade-level standards.		
D. Curricular materials are designed to include a variety of frequent, authentic application opportunities.		
4. Standards for Mathematical Practice		
A. Curricular materials support the standards' emphasis on mathematical thinking and reasoning.		

B. Curricular materials provide regular opportunities for students to engage in the full meaning of all the Standards for Mathematical Practice.		
C. Curricular materials support teachers in developing their own understanding of the Standards for Mathematical Practice, the role of the practice standards in lessons, and guidance for implementation.		
D. Curricular materials connect content standards and practice standards in authentic ways.		
5. Accessibility, Differentiation, and Engagement		
A. Curricular materials intentionally promote student engagement, student-to-student discourse, and student ownership of learning.		
B. Curricular materials ensure all students can access grade-level mathematics. i. Lesson tasks provide multiple entry points into mathematics. ii. Curricular materials provide timely supports to assess and to address students' unfinished learning.		
C. Curricular materials are designed with principles of Universal Design for Learning by providing multiple means of engagement, representation, and action and expression.		
D. Curricular materials provide scaffolds and instructional supports for multilingual learners.		
E. Curricular materials provide differentiation suggestions for support and challenge.		
F. Curricular materials attend to social and emotional learning (SEL) competencies: self-awareness, self-management, social awareness, relationship skills, and responsible decision-making.		
G. Curricular materials are inclusive and reflect diverse cultures, ethnicities, and demographics.		
H. Student facing-materials are visually engaging, accessible, and readable.		
6. Assessment Program		
A. Curricular materials include frequent and varied and comprehensive assessments. i. Summative assessments, taken as a whole, include opportunities for students to demonstrate the full intent of grade-level standards. ii. Formative assessments support teachers in determining whether students met the objective(s) of the lessons and topics. iii. Assessment items include a combination of tasks that require students to demonstrate conceptual understanding, procedural skill and fluency, and application. iv. Assessment item types require students to produce a variety of answers and solutions (arguments, explanations, representations, etc.		
B. Assessment materials provide sufficient guidance for interpreting student performance and guiding instructional decisions.		
7. Teachability and Digital Integration		
A. Curricular materials include embedded and external professional development. i. Materials support teacher learning and understanding of mathematical concepts, the progression of learning, and instructional pedagogy. ii. Materials include standards alignment information and explain the role of the standards in the resources.		
B. Curricular materials include support for implementation. i. The materials are visually engaging, easy to use, and well organized for students and teachers. ii. Materials provide information about how to plan and prepare lessons. iii. Materials provide guidance for instructional delivery, including questions to prompt student thinking and expected student outcomes.		

C. Curricular materials can be completed within a regular school year, and guidance about the expected timing for lessons and tasks is provided.		
D. Curricular materials provide caregivers with resources to support student academic progress.		
E. A user-friendly online platform provides always-on access to curricular materials and additional resources.		
F. Digital materials and experiences enhance classroom instructional practice, engaging students meaningfully to develop mathematical understanding.		

Criteria of High-Quality, Effective Math Programs	Evidence of Alignment from *Eureka Math²*		
	Yes	No	Criteria Examples and Reviewer Notes
1. Content and Focus			
A. Curricular materials align with standards and are mathematically accurate. i. Sufficient time and resources are allocated to ensure the materials meet the full intent of grade-level standards.			
B. Curricular materials focus on major work of each grade level.			Refer to the module maps, Appendix A.
C. Curricular materials connect supporting and additional work to major work in meaningful ways. i. Curricular materials make natural connections between different clusters and			

domains.			
2. Coherence and Instructional Design			
A. Curricular materials use a logical mathematical progression to build on learning from prior content.			
B. Coherent high-leverage models are evident within and across grade levels.			
C. Curricular materials include an intentional sequence for developing academic and mathematical language within and across grade-level courses.			
D. Curricular materials utilize a consistent module and lesson structure, including a variety of well-designed teacher-facilitated experiences.			
E. Students' ideas are valued and seen as resources for learning.			

F. Curricular materials build knowledge of not only key ideas in mathematics but also knowledge of the world.			
G. Curricular materials are research-based.			See Appendix B: Selection of Eureka Math^2 Research Citations.
3. Balance of Rigor			
A. Curricular materials contain a balance of conceptual understanding, procedural skills and fluency, as well as application of math knowledge.			
B. Curricular materials support the development of students' conceptual understanding with i. simple–to–complex problem sequences ii. concrete–pictorial–symbolic progressions and connections			

C. Curricular materials are designed so that students attain the procedural skills and fluency required by grade-level standards.			
D. Curricular materials are designed to include a variety of frequent authentic application opportunities.			
4. Standards for Mathematical Practice			
A. Curricular materials support the standards' emphasis on mathematical thinking and reasoning.			
B. Curricular materials provide regular opportunities for students to engage in the full meaning			

of all the Standards for Mathematical Practice.			
C. Curricular materials support teachers in developing their own understanding of the Standards for Mathematical Practice, the role of the practice standards in lessons, and guidance for implementation.			
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5. Accessibility, Differentiation, and Engagement			
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cs. ii. Curricular materials provide timely supports to assess and to address students' unfinished learning.			
C. Curricular materials are designed with principles of Universal Design for Learning by providing multiple means of engagement, representation, and action and expression.			
D. Curricular materials provide scaffolds and instructional supports for multilingual learners.			
E. Curricular materials provide differentiation suggestions for support and challenge.			

F. Curricular materials attend to social and emotional learning (SEL) competencies: self-awareness, self-management, social awareness, relationship skills, and responsible decision-making.			
G. Curricular materials are inclusive and reflect diverse cultures, ethnicities, and demographics.			
H. Student facing-materials are visually engaging, accessible, and readable.			
6. Assessment Program			
A. Curricular materials include frequent and varied and comprehensive assessments. i. Summative assessments, taken as a whole, include opportunities for			

students to demonstrate the full intent of grade-level standards. ii. Formative assessments support teachers in determining whether students met the objective(s) of the lessons and topics. iii. Assessment items include a combination of tasks that require students to demonstrate conceptual understanding, procedural skill and fluency, and application. iv. Assessment item types require students to produce a variety of answers and solutions (arguments, explanations, representations, etc.)			
B. Assessment materials provide sufficient guidance			

for interpreting student performance and guiding instructional decisions.			
7. Teachability and Digital Integration			
A. Curricular materials include embedded and external professional development. i. Materials support teacher learning and understanding of mathematical concepts, the progression of learning, and instructional pedagogy. ii. Materials include standards alignment information and explain the role of the standards in the resources.			

B. Curricular materials include support for implementation. i. The materials are visually engaging, easy to use, and well organized for students and teachers. ii. Materials provide information about how to plan and prepare lessons. iii. Materials provide guidance for instructional delivery, including questions to prompt student thinking and expected student outcomes.			
C. Curricular materials can be completed within a regular school year and guidance about the amount of time lessons and tasks may take is provided.			

D. Curricular materials provide caregivers with resources to support student academic progress.			
E. A user-friendly online platform provides always-on access to curricular materials and additional resources.			
F. Digital materials and experiences enhance classroom instructional practice, engaging students meaningfully to develop mathematical understanding.			

Appendix A

EUREKA MATH²

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Year-Long Curriculum Overview: Levels K–5

		STORY OF UNITS					
		Level K Part–Part–Total	**Level 1** Units of Ten	**Level 2** Ten Tens	**Level 3** Units of Any Number	**Level 4** Fractional Units	**Level 5** Fractions Are Numbers
Trimester 1	Quarter 1	**Module 1: Counting and Cardinality** 7 Topics | 33 Lessons	**Module 1: Counting, Comparison, and Addition** 4 Topics | 25 Lessons	**Module 1: Place Value Concepts through Metric Measurment and Data • Place Value, Counting, and Comparing Within 1,000** 9 Topics | 38 Lessons	**Module 1: Multiplication and Division with Units of 2, 3, 4, 5, and 10** 5 Topics | 23 Lessons	**Module 1: Place Value Concepts for Addition and Subtraction** 5 Topics | 24 Lessons	**Module 1: Place Value Concepts for Multiplication and Division with Whole Numbers** 4 Topics | 20 Lessons
	Quarter 2	**Module 2: Two- and Three-Dimensional Shapes** 3 Topics | 16 Lessons	**Module 2: Addition and Subtraction Relationships** 5 Topics | 23 Lessons	**Module 2: Addition and Subtraction Within 200** 4 Topics | 27 Lesons	**Module 2: Place Value Concepts through Metric Measurement** 4 Topics | 25 Lessons	**Module 2: Place Value Concepts for Multiplication and Division** 5 Topics | 26 Lessons	**Module 2: Addition and Subtraction with Fractions** 4 Topics | 17 Lessons
Trimester 2		**Module 3: Comparison** 4 Topics | 22 Lessons	**Module 3: Properties of Operations to Make Easier Problems** 5 Topics | 26 Lessons	**Module 3: Shapes and Time with Fraction Concepts** 4 Topics | 19 Lesons	**Module 3: Multiplication and Division with Units of 0, 1, 6, 7, 8, and 9** 4 Topics | 25 Lessons	**Module 3: Multiplication and Division of Multi-Digit Numbers** 6 Topics | 24 Lessons	**Module 3: Multiplication and Division with Fractions** 4 Topics | 22 Lessons
	Quarter 3	**Module 4: Composition and Decomposition** 3 Topics | 18 Lessons	**Module 4: Comparison and Composition of Length Measurements** 3 Topics | 14 Lessons	**Module 4: Addition and Subtraction Within 1,000** 5 Topics | 24 Lessons	**Module 4: Multiplication and Area** 4 Topics | 19 Lessons	**Module 4: Foundations for Fraction Operations** 6 Topics | 34 Lessons	**Module 4: Place Value Concepts for Decimal Operations** 5 Topics | 30 Lessons
		Module 5: Addition and Subtraction 4 Topics | 27 Lessons	**Module 5: Place Value Concepts to Compare, Add, and Subtract** 5 Topics | 25 Lessons	**Module 5: Money, Data, and Customary Measurement** 3 Topics | 16 Lessons	**Module 5: Fractions as Numbers** 5 Topics | 27 Lessons		**Module 5: Addition and Multiplication with Area and Volume** 4 Topics | 28 Lessons
Trimester 3	Quarter 4	**Module 6: Place Value Foundations** 4 Topics | 24 Lessons	**Module 6: Attributes of Shapes • Advancing Place Value, Addition, and Subtraction** 6 Topics | 31 Lessons	**Module 6: Multiplication and Division Foundations** 4 Topics | 18 Lessons	**Module 6: Geometry, Measurement, and Data** 4 Topics | 26 Lessons	**Module 5: Place Value Concepts for Decimal Fractions** 4 Topics | 14 Lessons **Module 6: Angle Measurements and Plane Figures** 4 Topics | 20 Lessons	**Module 6: Foundations to Geometry in the Coordinate Plane** 4 Topics | 20 Lessons
		TOTAL: 25 Topics | 140 Lessons	**TOTAL:** 28 Topics | 144 Lessons	**TOTAL:** 29 Topics | 142 Lessons	**TOTAL:** 26 Topics | 145 Lessons	**TOTAL:** 30 Topics | 142 Lessons	**TOTAL:** 25 Topics | 137 Lessons

Trimester and quarter indicators are provided as a guide for pacing. A few optional lessons in each grade level are included in the total number of lessons. About thirty additional days are allotted at each level for assessment and responsive teaching.

012022

EUREKA MATH²

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Year-Long Curriculum Overview: Level 6–Algebra I

		STORY OF RATIOS			STORY OF FUNCTIONS
		Level 6 Ratios and Rates	**Level 7** Ratios and Proportionality	**Level 8** Ratios and Linearity	**Algebra I** Modeling with Functions
Trimester 1	Quarter 1	**Module 1: Ratios, Rates, and Percents** 5 Topics | 26 Lessons	**Module 1: Ratios and Proportional Relationships** 3 Topics | 20 Lessons	**Module 1: Scientific Notation, Exponents, and Irrational Numbers** 5 Topics | 24 Lessons	**Module 1: Expressions, Equations, and Inequalities in One Variable** 4 Topics | 23 Lessons
	Quarter 2	**Module 2: Operations with Fractions and Multi-Digit Numbers** 6 Topics | 24 Lessons	**Module 2: Operations with Rational Numbers** 5 Topics | 26 Lessons	**Module 2: Rigid Motions and Congruent Figures** 4 Topics | 22 Lessons	**Module 2: Equations and Inequalities in Two Variables** 4 Topics | 24 Lessons
Trimester 2		**Module 3: Rational Numbers** 4 Topics | 17 Lessons	**Module 3: Expressions, Equations, and Inequalities** 4 Topics | 23 Lessons	**Module 3: Dilations and Similar Figures** 4 Topics | 17 Lessons	**Module 3: Functions and Their Representations** 4 Topics | 23 Lessons
	Quarter 3	**Module 4: Expressions and One-Step Equations** 5 Topics | 25 Lessons	**Module 4: Geometry** 5 Topics | 26 Lessons	**Module 4: Linear Equations in One and Two Variables** 6 Topics | 27 Lessons	**Module 4: Quadratic Functions** 4 Topics | 27 Lessons
Trimester 3		**Module 5: Area, Surface Area, and Volume** 4 Topics | 19 Lessons	**Module 5: Percent and Applications of Percent** 5 Topics | 24 Lessons	**Module 5: Systems of Linear Equations** 3 Topics | 14 Lessons	**Module 5: Linear and Exponential Functions** 4 Topics | 24 Lessons
	Quarter 4	**Module 6: Statistics** 4 Topics | 22 Lessons	**Module 6: Probability and Populations** 4 Topics | 19 Lessons	**Module 6: Functions and Bivariate Statistics** 5 Topics | 25 Lessons	**Module 6: Modeling with Functions** 2 Topics | 7 Lessons
		TOTAL: **28 Topics | 133 Lessons**	**TOTAL:** **26 Topics | 138 Lessons**	**TOTAL:** **27 Topics | 129 Lessons**	**TOTAL:** **22 Topics | 128 Lessons**

Trimester and quarter indicators are provided as a guide for pacing. A few optional lessons in each grade level/course are included in the total number of lessons. About thirty additional days are allotted at each level for assessment and responsive teaching.

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Appendix B: Selection of *Eureka Math²* Research Citations

Berlinghoff, W. P. and F. Q. Gouvêa. *Math through the Ages: A Gentle History for Teachers and Others*. Farmington, ME: Oxton House Publishers, 2002.

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